

CHAPITRE 0 : RENTRÉE

Correction

On effectue directement le calcul de A sans développer. On a

$$\begin{aligned} A &= (3 - \sqrt{2})(1 + \sqrt{2}) - (1 + \sqrt{2})^2 \\ &= [(3 - \sqrt{2}) - (1 + \sqrt{2})](1 + \sqrt{2}) \\ &= (2 - 2\sqrt{2})(1 + \sqrt{2}) = 2(1 - \sqrt{2})(1 + \sqrt{2}) \\ &= 2(1^2 - (\sqrt{2})^2) = 2(1 - 2) = -2. \end{aligned}$$

On calcule B en développant. On a

$$\begin{aligned} B &= (-1 + 5\sqrt{2})(-4 + 3\sqrt{2}) + (11 - \sqrt{2})^2 + 45\sqrt{2} - 145 \\ &= (4 - 3\sqrt{2} - 20\sqrt{2} + 30) + (121 - 22\sqrt{2} + 2) + 45\sqrt{2} - 145 \\ &= (4 + 30 + 121 + 2 - 145) + (-3 - 20 - 22 + 45)\sqrt{2} \\ &= 12. \end{aligned}$$